

# Securitized Markets, International Capital Flows, and Global Welfare

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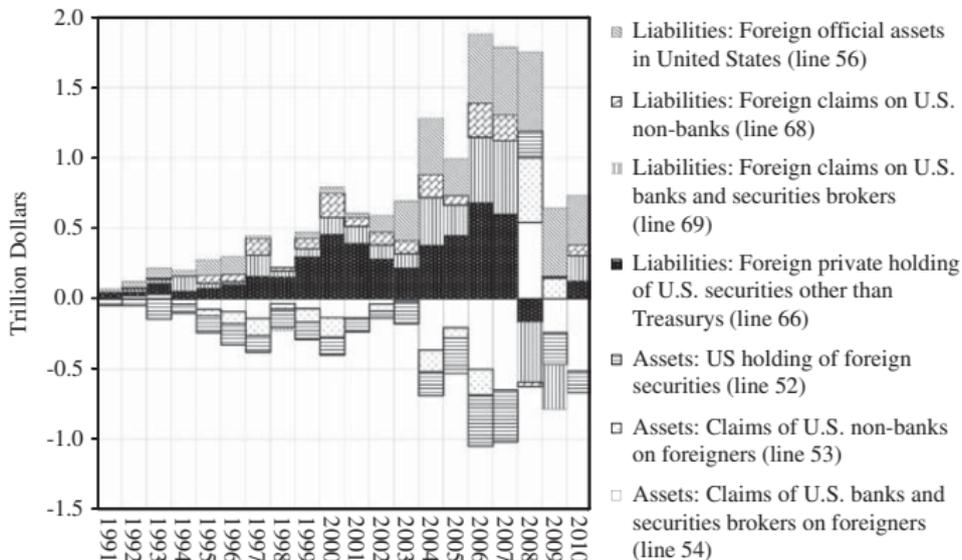
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SWET Conference  
August 7, 2016

# Gross Financial Flows

From Shin (2012)

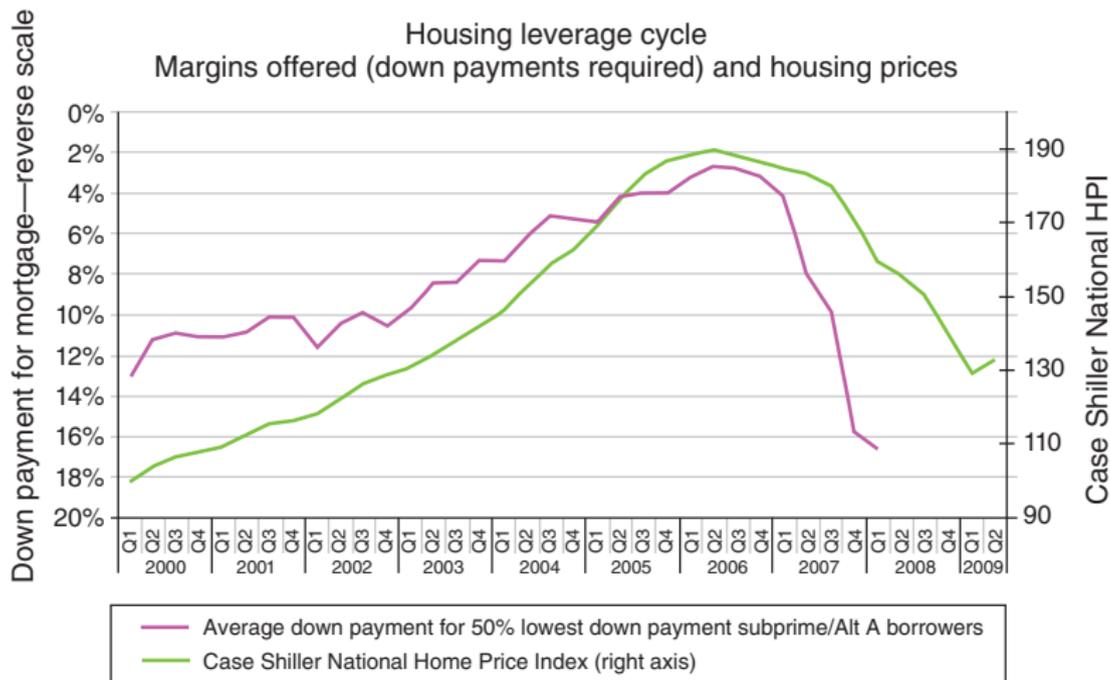
Figure 2. U.S. Gross Capital Flows by Category



Source: U.S. Bureau of Economic Analysis. Increase in U.S. liability to foreigners is indicated by positive bar, increase in U.S. claims on foreigners is indicated by negative bar. Only a subset of gross flows is included, so that flows do not sum to zero.

# Leverage in Housing Markets

From Fostel & Geanakoplos (2012)



# Introduction

## Background

- Proliferation of securitized financial markets since 90's
- Net and gross capital flows into U.S. increased persistently until 2007 and collapsed following the 2007–2009 financial crisis
- Loan down payments in the U.S. very low pre-crisis, very high post-crisis

## Question

1. How do securitized markets affect international capital flows?
2. What are effects on welfare, growth, and inequality?

# Contribution

## What we do

- Develop a two country general equilibrium model with uninsurable idiosyncratic investment risk and securitized loan markets
- Study the effect of financial integration on capital flows, growth, welfare, and inequality

## Main results

1. Capital flows from high-margin (Foreign) to low-margin (Home) country
2. Upon financial integration,
  - Home: interest rate  $\downarrow$ , growth  $\uparrow$ , inequality  $\uparrow$
  - Foreign: welfare  $\uparrow$ , growth  $\downarrow$ , inequality  $\downarrow$

## Intuition

- Foreign demands “safe enough” assets
- Home can endogenously supply “safe enough” assets through more lending and high leverage

## Related Literature

- **“Global Imbalances”**: Willen (2004), Caballero, Farhi, & Gourinchas (2008), Mendoza, Quadrini, & Ríos-Rull (2009), Angeletos & Panousi (2011), Maggiori (2015)
- **Capital Flows**: Gourinchas & Jeanne (2006), Caballero & Krishnamurthy (2009), Bertaut, DeMarco, Kamin, & Tryon (2012), Obstfeld (2012), Shin (2012)
- **Collateral Equilibrium**: Geanakoplos (1997, 2003), Fostel & Geanakoplos (2008, 2012), Fostel, Geanakoplos, & Phelan (2015), Toda (2013)

# Setup

- Two countries, Home and Foreign
- Two periods,  $t = 0, 1$
- Unit continuum of ex ante identical entrepreneurs indexed by  $i \in [0, 1]$  with risky investment projects
- Unit continuum of financial intermediaries (risk-neutral, perfectly competitive, profit-maximizing) who service loans and issue asset-backed securities (ABS)

## Entrepreneurs/Investors

- Identical preferences over final consumption

$$U(C) = E[u(C)],$$

where  $u' > 0$ ,  $u'' < 0$

- Agents in country  $j = H, F$  endowed with  $W^j$  units of capital good at  $t = 0$ , no endowment at  $t = 1$
- Linear investment technology with stochastic productivity  $A^i$ 
  - Investor  $i$ 's investment of  $k^i$  yields  $A^i k^i$  in  $t = 1$
  - $A^i \sim$  i.i.d. across agents (no aggregate risk for now)

## Financial Structure: Collateralized Loans

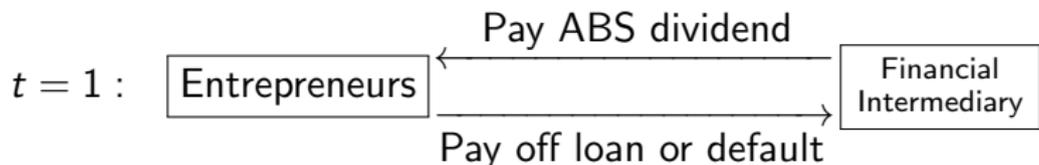
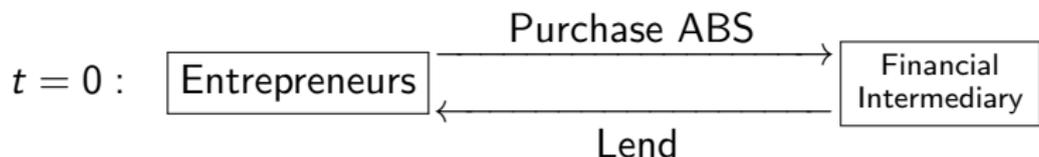
- Markets are incomplete: investors can only borrow from intermediary using loan by putting up their investments as collateral
- A loan in country  $j$  is characterized by (exogenous) collateral requirement  $c_j \geq 1$  (down payment  $d_j = 1 - 1/c_j$ ) and (equilibrium) borrowing rate  $R_b^j$ ; **assume  $c_H < c_F$**
- For each dollar borrowed, entrepreneur in country  $j$  must invest  $c_j$  dollars in the project and put up its return,  $A^i c_j$ , as collateral
- Loans are non-recourse: agent  $i$  in country  $j$  delivers

$$\min \left\{ A^i c_j, R_b^j \right\}$$

for each dollar borrowed

## Financial Structure: ABS

- Financial intermediaries lend to entrepreneurs and pool loan contacts to issue asset-backed securities (ABS)
- Closest thing in real world is collateralized loan obligations (CLO)
- Perfect competition implies ABS are pass-through securities that pay  $R_{ABS}^j = E \left[ \min \left\{ A^i c_l, R_b^j \right\} \right]$



## Portfolio

- Agents can borrow only from domestic loans but can invest in ABS of either country
- Portfolio in country  $j$  denoted by  $\pi^j = (\theta^j, \phi_H^j, \phi_F^j, \psi^j)$ , where
  - $\theta^j \geq 0$ : fraction of capital invested in the risky project
  - $\phi_H^j$  ( $\phi_F^j$ )  $\geq 0$ : fraction invested in Home (Foreign) asset-backed security
  - $\psi^j \geq 0$ : fraction borrowed from loan
- Budget constraint is

$$\theta^j + \phi_H^j + \phi_F^j - \psi^j = 1$$

- Collateral constraint is

$$\theta^j \geq c_j \psi^j$$

## Equilibrium and Properties

- A collateral equilibrium with ABS is defined by borrowing rates and portfolio choices such that (i) agents optimize and (ii) markets clear
- Since there are no aggregate shocks, all ABS pools are risk-free (idiosyncratic risks are diversified away)
  - In autarky equilibrium, markets clear in each country (with different risk-free rates)
  - In financial integration equilibrium, markets clear globally (with identical risk-free rates but not borrowing rates)

# Equilibrium and Properties

## Proposition

*Consider a country with autarky risk-free rate  $R_f^{\text{Aut}}$ . If the country faces a higher interest rate  $R_f^{\text{Int}} > R_f^{\text{Aut}}$  after financial integration, then the country reduces real investment  $\theta$ , increases investment in the ABS  $\phi$ , and reduces borrowing  $\psi$ . Furthermore, the country gains from financial integration in terms of welfare.*

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Intuition:

- Since  $R_f = E[\min \{A^i c, R_b\}]$ , risk-free rate and borrowing rate move in same direction
- Since  $\min \{A^i c, R_b\} = c \min \{A^i, R_b/c\}$ , default threshold is  $R_b/c$  (non-recourse loan is essentially convertible bond)
- Hence higher interest rates improve welfare because more down side risk sharing (**endogenous risk sharing**)

## Equilibrium and Properties

### Theorem

Suppose that  $R_f^{\text{Int}} > R_f^{F,\text{Aut}}$ . Then  $R_f^{\text{Int}} < R_f^{H,\text{Aut}}$ ,

1. Home increases and Foreign decreases real investment:

$$\theta^{H,\text{Int}} > \theta^{H,\text{Aut}} = 1 = \theta^{F,\text{Aut}} > \theta^{F,\text{Int}},$$

2. Home decreases and Foreign increases investment in ABS:

$$\sum_{j=H,F} \phi_j^{H,\text{Int}} < \phi^{H,\text{Aut}}, \quad \sum_{j=H,F} \phi_j^{F,\text{Int}} > \phi^{F,\text{Aut}},$$

3. Home increases and Foreign decreases borrowing:

$$\psi^{H,\text{Int}} > \psi^{H,\text{Aut}}, \quad \psi^{F,\text{Int}} < \psi^{F,\text{Aut}},$$

4. The global supply of safe assets increases:

$$\frac{W^H \theta^{H,\text{Int}}}{c^H} + \frac{W^F \theta^{F,\text{Int}}}{c^F} > \frac{W^H \theta^{H,\text{Aut}}}{c^H} + \frac{W^F \theta^{F,\text{Aut}}}{c^F} = \frac{W^H}{c^H} + \frac{W^F}{c^F}.$$

## Welfare Implications

- By previous results, Foreign gains from financial integration
- Home welfare is ambiguous

### Proposition

*Suppose that Foreign wealth  $W^F$  is sufficiently large. Let  $V^{H, \text{Aut}}$ ,  $V^{H, \text{Int}}$  be the Home welfare in autarky and after financial integration.*

- 1. If Home collateral requirement  $c_H$  is sufficiently low and  $u(\infty) = \infty$ , then Home welfare after financial integration exceeds the complete market level (perfect risk sharing):  $V^{H, \text{Int}} > u(E[A^i]W^H)$ .*
- 2. If  $u$  is CRRA with relative risk aversion  $\gamma > 1$  sufficiently large, then Home loses from financial integration:  $V^{H, \text{Int}} < V^{H, \text{Aut}}$ .*

Intuition: **endogenous risk sharing**

## Numerical Example

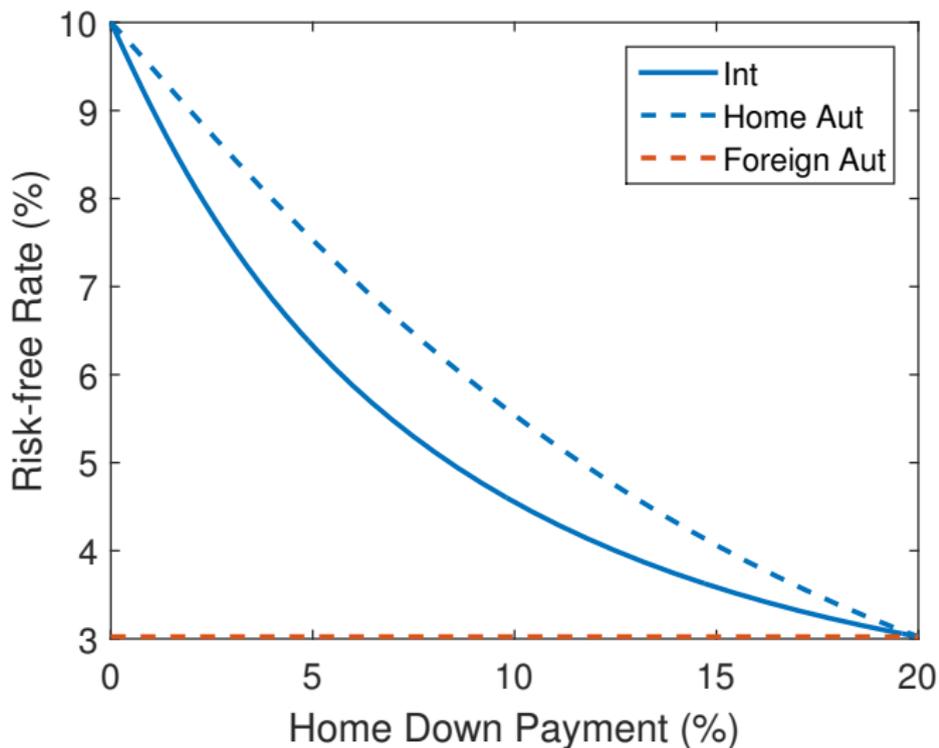
- Utility is CRRA,  $u(C) = \frac{1}{1-\gamma} C^{1-\gamma}$ , with  $\gamma = 2$
- Productivities are log-normally distributed,

$$\log A^i \sim N(\mu - \sigma^2/2, \sigma^2),$$

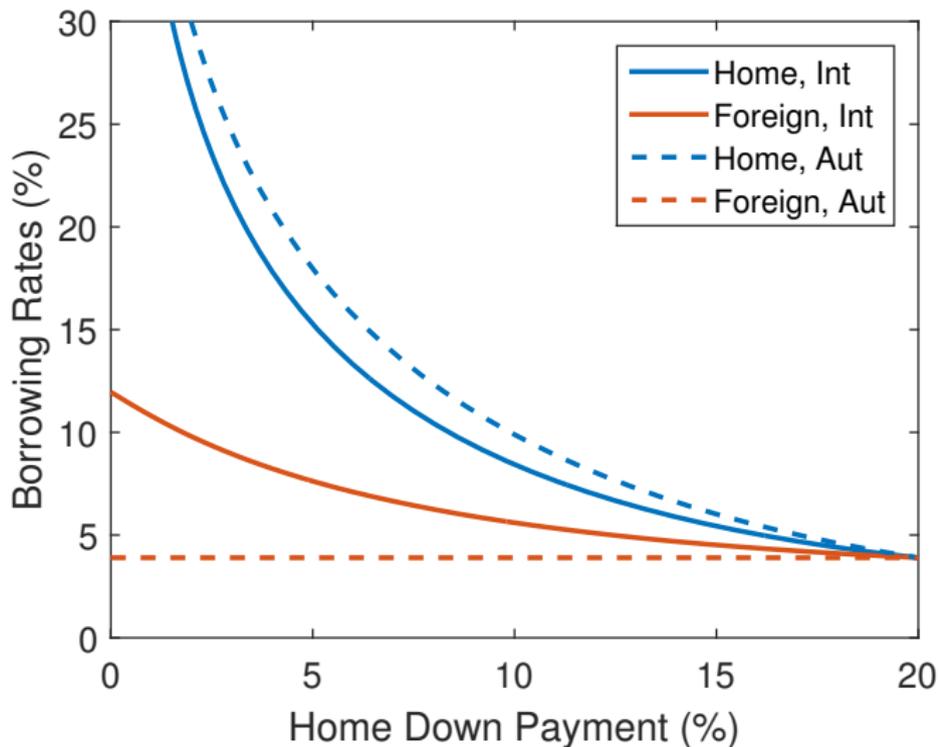
with  $e^\mu = 1.1$  (expected return = 10%) and  $\sigma = 20\%$

- $c_F = 1.25$  (down payment = 20%)
- Vary  $c_H \in [1, 1.25]$  (down payment  $\in [0, 20\%]$ )

## Risk-free rates



## Borrowing rates

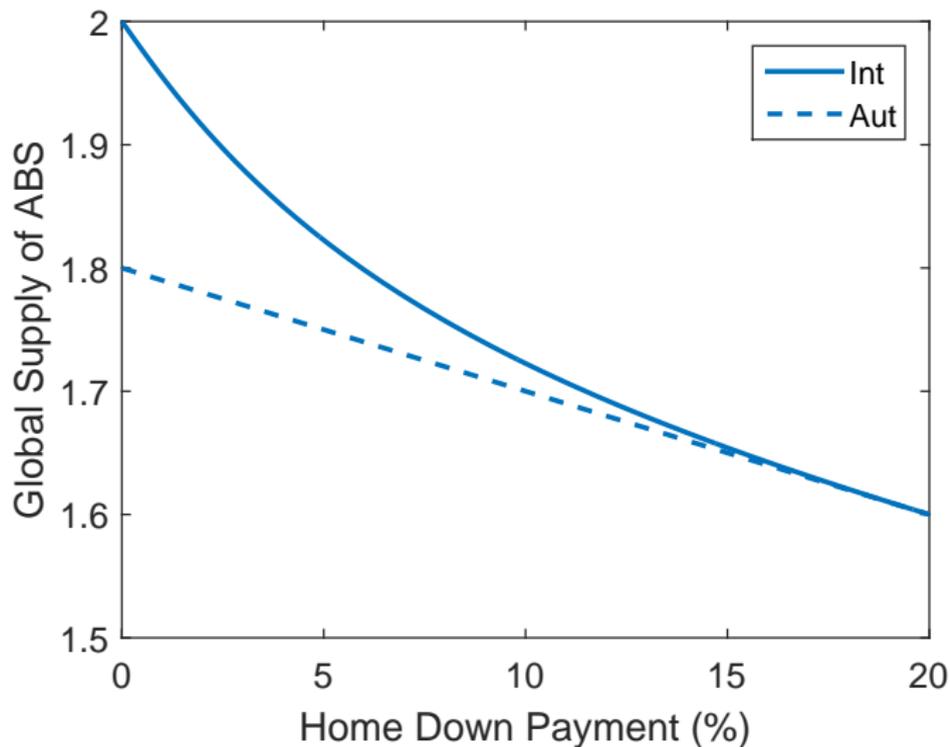








## Global supply of safe assets



## Changes in Welfare

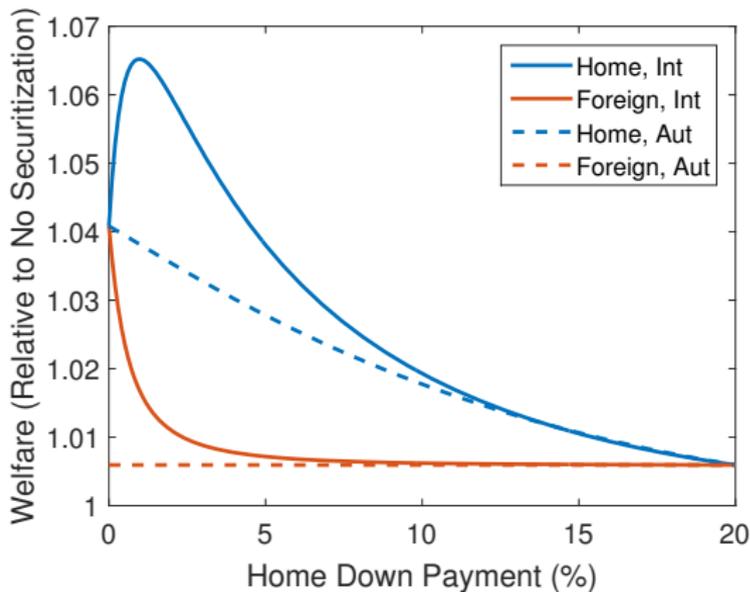
- Models in existing literature get different welfare results (different financial frictions and financial structures)
- In those models the degree of risk sharing is not affected by financial integration—always the same fraction of idiosyncratic risk that is insured
- In our model the degree of risk sharing is endogenous:

$$A^i c \geq R_b \iff A^i \geq R_b / c,$$

so default threshold (degree of risk sharing) depends on borrowing rate  $R_b$

## “Saving Glut” Economy

- Risk sharing depends endogenously on the changes in interest rates, which depend on the size of capital flows
- Consider when Foreign is much larger (9 times Home, “saving glut”) to better understand how capital flows affect welfare



## Introducing Aggregate Risks

▶ Skip aggregate risks

- Aggregate states,  $s = 1, \dots, S$ , occurring with probability  $p_s$
- States index the distribution of payoffs to investors' projects  $F_s(\cdot)$
- To isolate the effect of securitization on international flows, we assume that the productivity distributions in each country are the same ("world shocks")
- Gross return on country  $j$ 's ABS in state  $s$  is

$$R_{\text{ABS}}^j(s) = E \left[ \min \left\{ A_{c_j}, R_b^j \right\} \mid s \right] = \int_0^\infty \min \left\{ c_j x, R_b^j \right\} dF_s(x)$$

## Nature of Shocks

- For simplicity we consider 2 aggregate states for numerical examples
- Consider two types of aggregate shocks:
  1. First-moment: expected return

$$\begin{aligned}E[A^i | s = 1] &> E[A^i | s = 2] \\ \text{Var}[A^i | s = 1] &= \text{Var}[A^i | s = 2]\end{aligned}$$

2. Second-moment: variance of returns

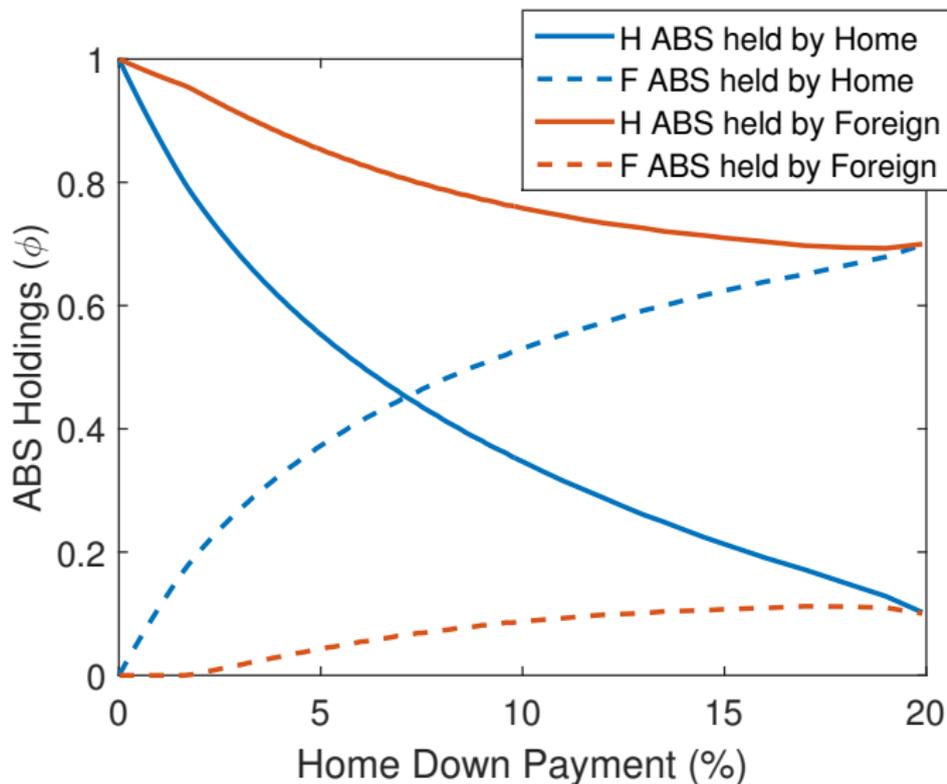
$$\begin{aligned}E[A^i | s = 1] &= E[A^i | s = 2] \\ \text{Var}[A^i | s = 1] &< \text{Var}[A^i | s = 2]\end{aligned}$$

## Numerical Example: First-Moment Shocks

- States equiprobable,  $p_1 = p_2 = 0.5$ 
  - $\mu_1 = 20\%$ ,  $\mu_2 = 0$
  - $\sigma_1 = \sigma_2 = 20\%$
- Equilibrium with first-moment shocks essentially the same
  - Investment essentially identical
  - Welfare changes from integration essentially identical
- Portfolio holdings of Home and Foreign ABS are not indeterminate—not both risk-free, not perfectly substitutable
- Results are robust to size of first-moment shock

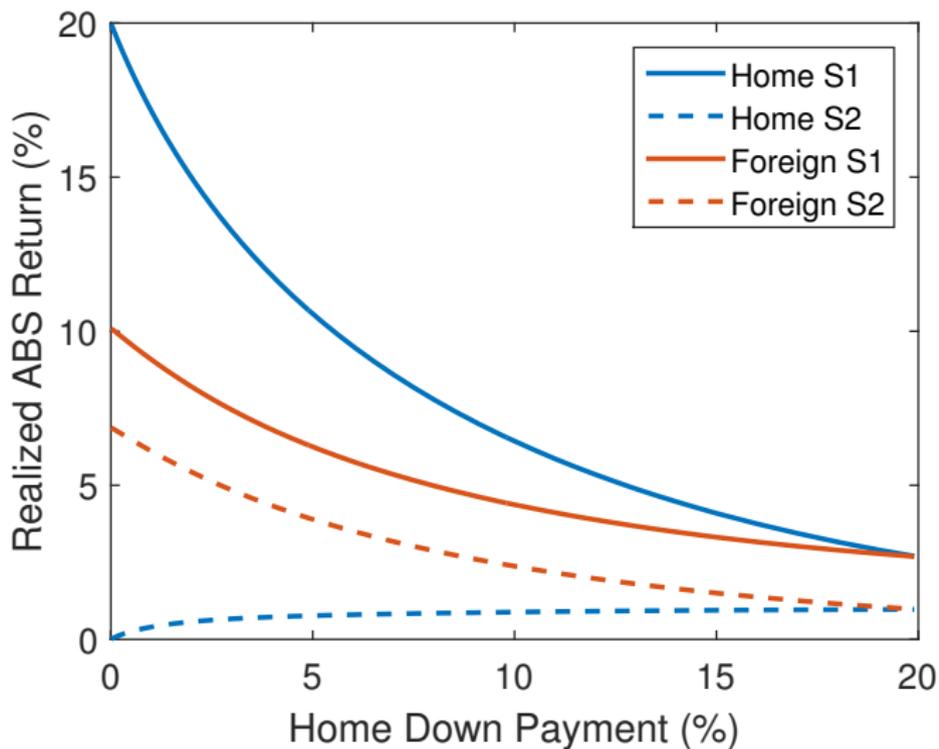
# Equilibrium with Financial Integration

## First-moment Shocks: ABS Holdings



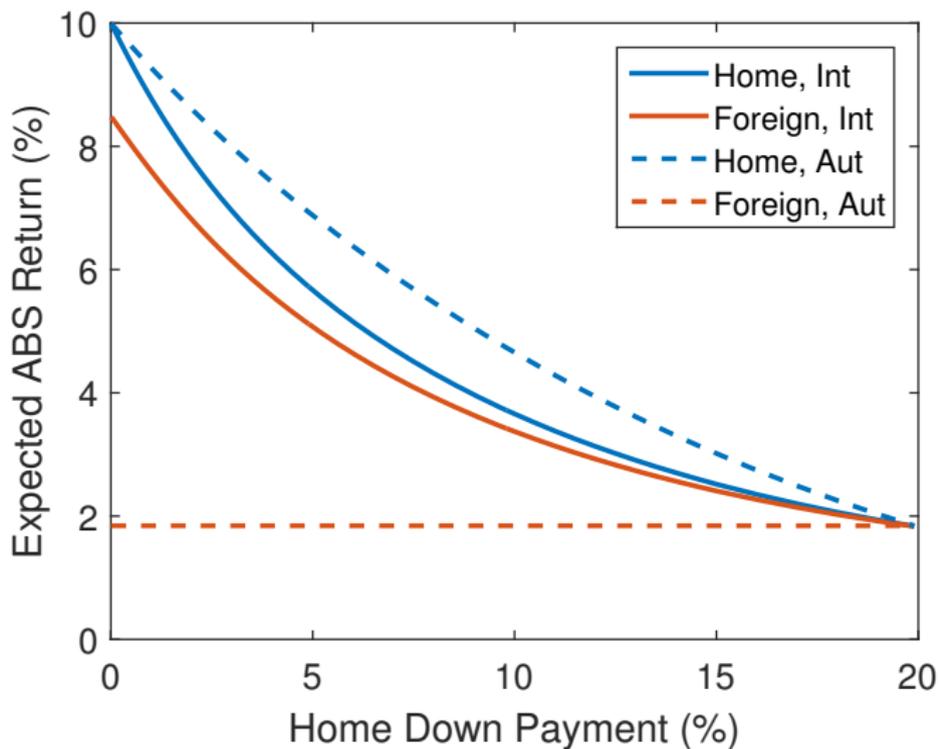
# Equilibrium with Financial Integration

First-moment Shocks: Realized ABS Returns



# Equilibrium with Financial Integration

First-moment Shocks: Expected ABS Returns



## ABS Flows with First-Moment Shocks

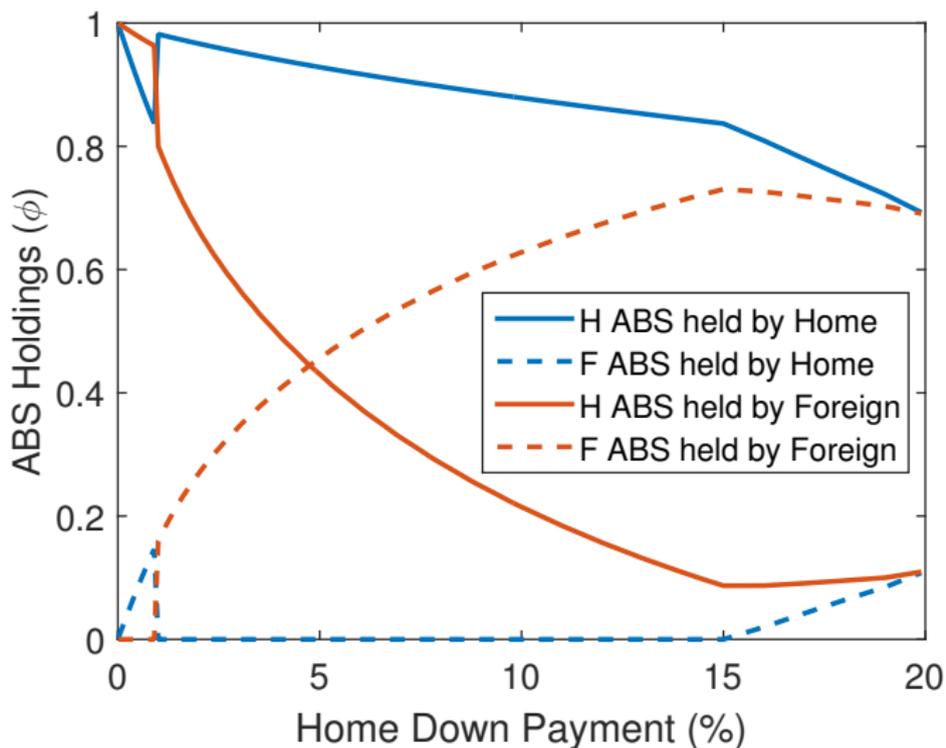
- With aggregate risk Home and Foreign ABS are not identical
  - Home ABS is riskier than Foreign (lower collateral rate)
  - Foreign investors typically hold ABS from both countries (except when they would like to short Foreign ABS)
  - Home investors hold Foreign ABS even though Foreign capital net flows into Home (gross flows)
- Foreign demand is for “safe enough” assets—safer than idiosyncratic investments—not for “safer” assets

## Numerical Example: Second-Moment Shocks

- States equiprobable,  $p_1 = p_2 = 0.5$ 
  - $\mu_1 = \mu_2 = 10\%$
  - $\sigma_1 = 10\%$ ,  $\sigma_2 = 30\%$
- Implications for gross flows entirely different
- With second-moment shocks gross flows collapse (no change in net flows)
- Results are robust to size of second-moment shock

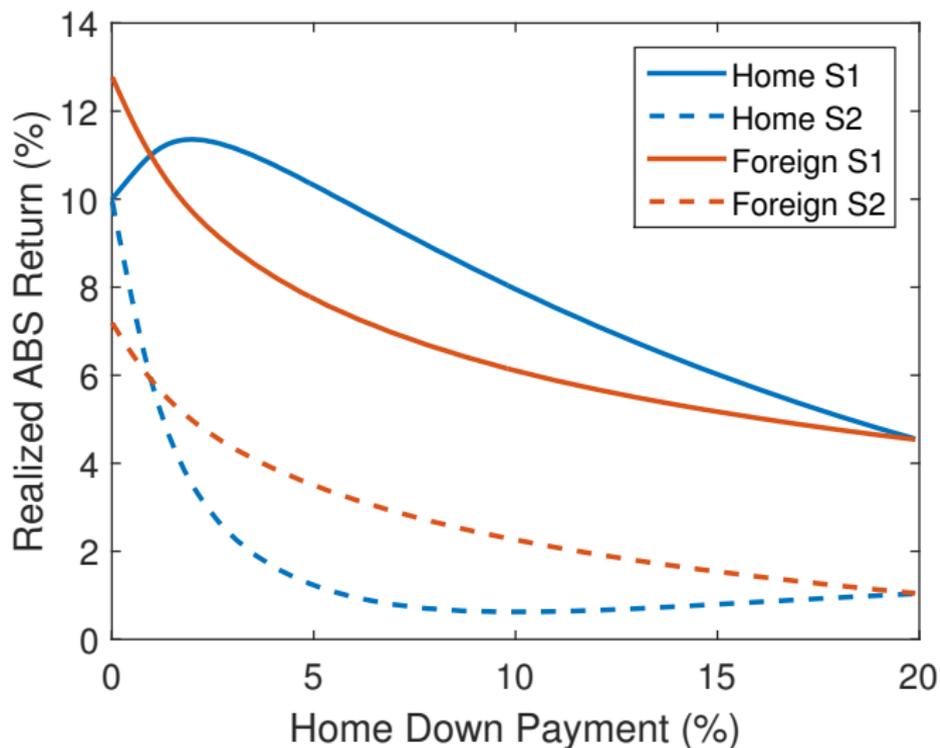
# Equilibrium with Financial Integration

## Second-moment Shocks: ABS Holdings



# Equilibrium with Financial Integration

## Second-moment Shocks: Realized ABS Returns



# Tranching

- We also consider effects of tranching (splitting ABS into state-contingent payoffs)—meaningful when non-negativity constraint binds
- Tranching yields complete markets for aggregate states  
     $\implies$  indeterminate portfolios
- Any degree of home-bias would cause gross flows to be zero
- Very small effects on welfare

## Model

- Infinite horizon:  $t = 0, 1, \dots$ ; productivity  $A_t^i$  i.i.d. across agents and time
- To separate portfolio choice (relative risk aversion, RRA) from saving (elasticity of intertemporal substitution, EIS), assume Epstein-Zin preferences:

$$U_t = \left( (1 - \beta) C_t^{1-1/\varepsilon} + \beta \mathbb{E}[U_{t+1}^{1-\gamma}]^{\frac{1-1/\varepsilon}{1-\gamma}} \right)^{\frac{1}{1-1/\varepsilon}}$$

where  $\gamma$ : RRA,  $\varepsilon$ : EIS

- Optimal portfolio problem:  $\rho = \max \mathbb{E}[R^i(\pi)^{1-\gamma}]^{\frac{1}{1-\gamma}}$ , where  $R^i(\pi)$ : agent  $i$ 's return on wealth with portfolio  $\pi$
- Remaining consumption problem is standard (calculus): solution is  $C_t = (1 - \beta^\varepsilon \rho^{1-\varepsilon}) W_t$

## Stationary Distribution

- If agents are infinitely lived, stationary distribution does not exist because shocks permanent
  - ⇒ Assume agents go bankrupt at probability  $\delta$  each period
- If newborn agents inherit capital, then one country will dominate in the long run because growth rates differ
  - ⇒ Assume agents are born with fixed capital and start private businesses, and capital of bankrupted agents wiped out

## Stationary Distribution

- Evolution of individual wealth:  $W_{i,t+1} = \beta^\varepsilon \rho^{1-\varepsilon} R_{t+1}^i(\pi) W_{it}$
- Gibrat's law, hence by Toda (JET, 2014), stationary distribution is (approximately) **double Pareto**
- Power law exponents  $-\alpha_1, \alpha_2$  are solutions to

$$\frac{\sigma^2}{2} \zeta^2 - \mu \zeta - \delta = 0,$$

where

$$\begin{aligned} \mu &= \log(\beta^\varepsilon \rho^{1-\varepsilon}) + \mathbb{E}[\log R^i(\pi)], \\ \sigma^2 &= \text{Var}[\log R^i(\pi)] \end{aligned}$$

- Steady state aggregate wealth:  $W = \frac{\delta}{1 - (1-\delta)\beta^\varepsilon \rho^{1-\varepsilon} \mathbb{E}[R^i(\pi)]} W_0$

# Equilibrium and Properties

## Proposition

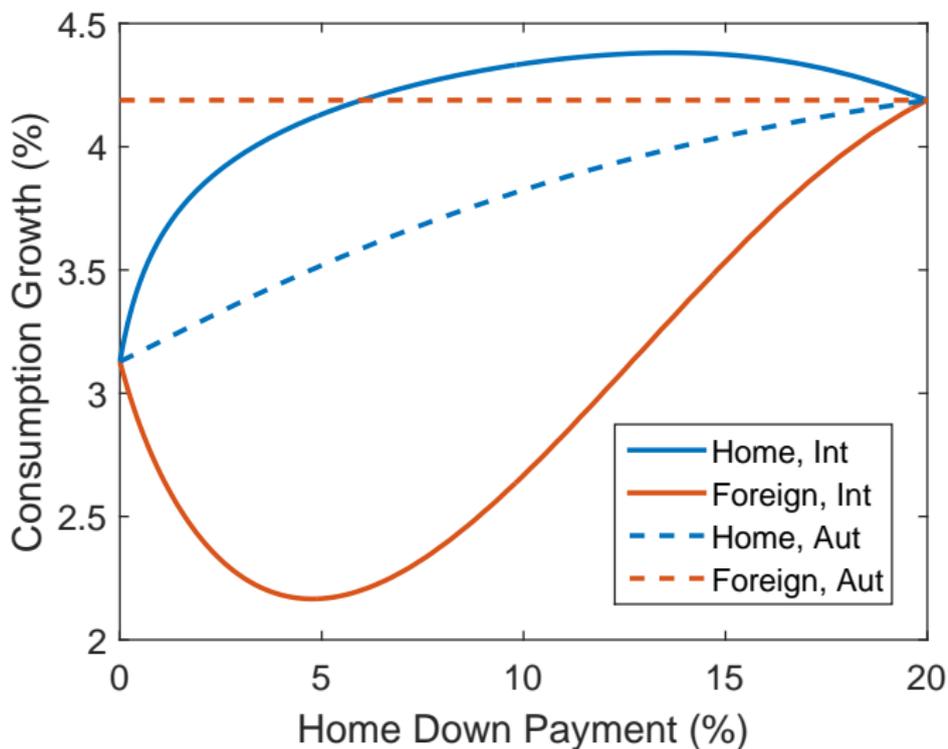
*Suppose that  $\varepsilon \leq 1$ . If a country faces a higher risk-free rate after financial integration, then the growth rate of individual wealth goes down and the steady state capital stock becomes lower than autarky.*

- Foreign will typically experience a slower economic growth

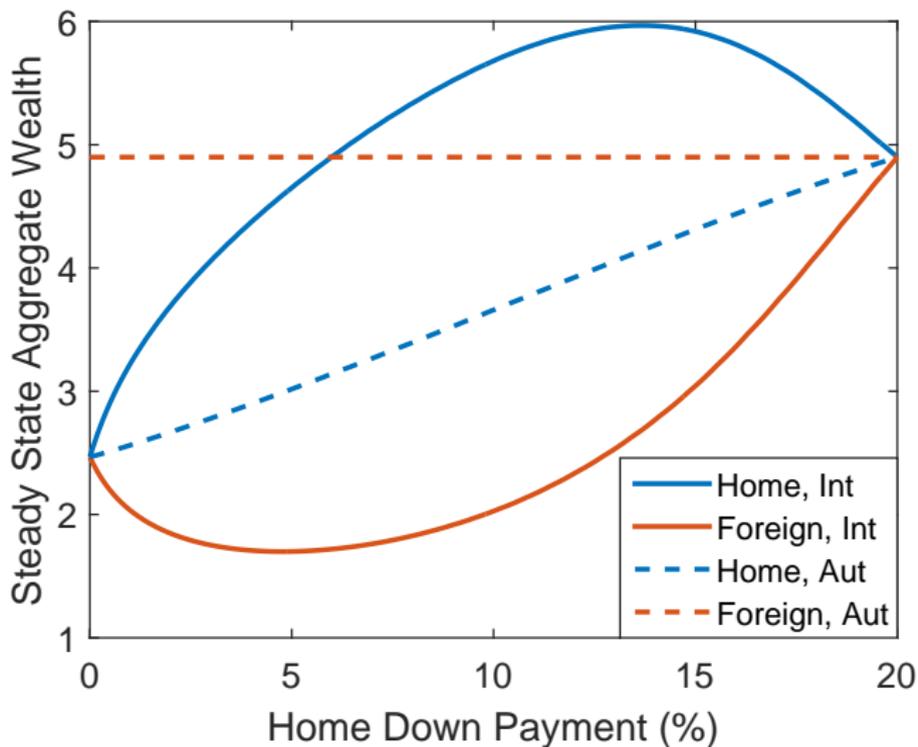
## Numerical Example: Growth and Inequality

- No aggregate risk, same parameters as before
- We set  $\varepsilon = 0.7$ ,  $\beta = 0.95$ , and  $\delta = 0.05$   
(average lifetime of private business  $1/0.05 = 20$  years)

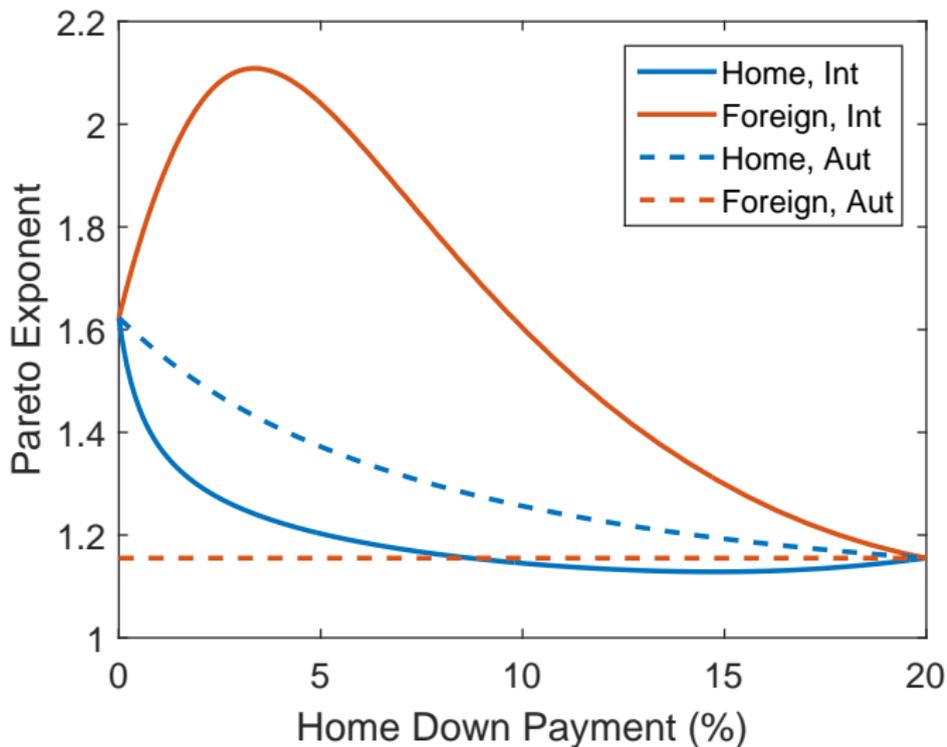
## Wealth Growth of Surviving Agents



# Steady State Aggregate Wealth



# Power Law Exponents



## Conclusion

- Different collateral requirements across countries lead to net international capital flows from high-margin to low-margin country
- Supply of safe assets and degree of risk sharing endogenously depend on financial integration and size of financial flows
- Foreign demand for “safe-enough” assets—Home doesn’t produce safer assets
- Gross flows depend on nature of aggregate shocks
- Financial integration has asymmetric effects on welfare, benefiting high-margin country